

# Modeling and optimization of multimodal urban networks with limited parking and dynamic pricing

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Riverside, Jan. 17<sup>th</sup>, 2015

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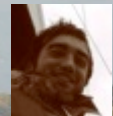


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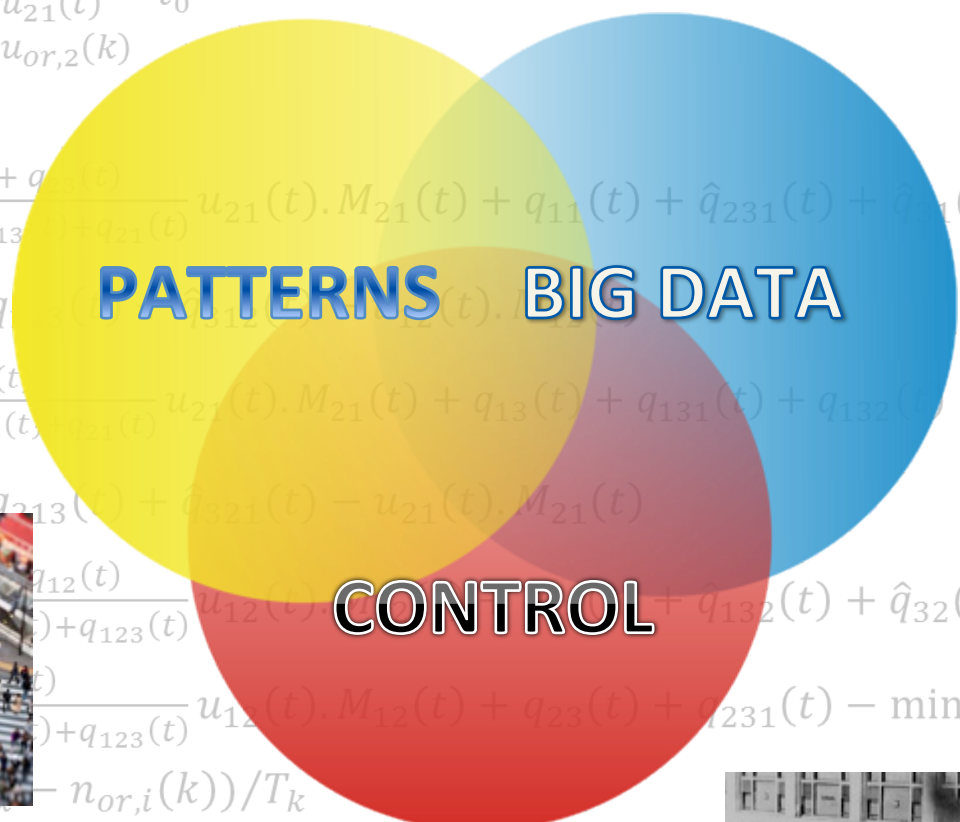


**Mehmet Yildirimoglu (CE)**





# A holistic approach of mobility



**PATTERNS** **BIG DATA**

**CONTROL**

$$\int_{t_0}^{t_f} [n_1(t) + n_2(t)] dt + \sum_{k=0}^{K-1} \sum_{l=1}^L x_l(k)$$

$$\frac{dn_{12}(t)}{dt} = q_{12}(t) + q_{21}(t) - u_{21}(t) \cdot M_{21}(t) + q_{11}(t) + \hat{q}_{231}(t) + \hat{q}_{11}(t)$$

$$\frac{dn_{13}(t)}{dt} = \frac{q_{213}(t)}{\hat{q}_{321}(t) + q_{213}(t)} u_{21}(t) \cdot M_{21}(t) + q_{13}(t) + q_{131}(t) + q_{132}(t) - \min(M_{13}(t), C_{or,1}(t))$$

$$\frac{dn_{21}(t)}{dt} = q_{21}(t) + q_{213}(t) + \hat{q}_{321}(t) - u_{21}(t) \cdot M_{21}(t)$$

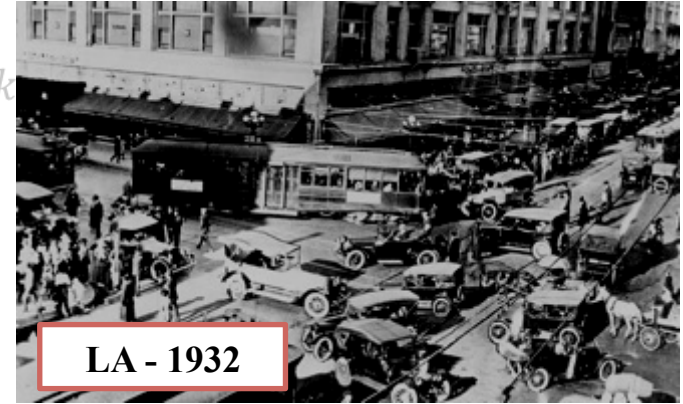
$$\frac{dn_{12}(t)}{dt} + q_{123}(t) + q_{12}(t) + q_{123}(t) u_{12}(t) \cdot M_{12}(t) + q_{23}(t) + q_{231}(t) - \min(M_{23}(t), C_{or,2}(t))$$

$$- n_{or,i}(k) / T_k$$

$$u_{min} \leq u_{12}(t), u_{21}(t) \leq u_{max}; u_{min} \leq u_{or,1}(k), u_{or,2}(k)$$

$$0 \leq n_1(t) + n_{11}(t) + n_{12}(t) + n_{13}(t)$$

$$0 \leq n_2(t) + n_{21}(t) + n_{22}(t) + n_{23}(t)$$



LA - 1932

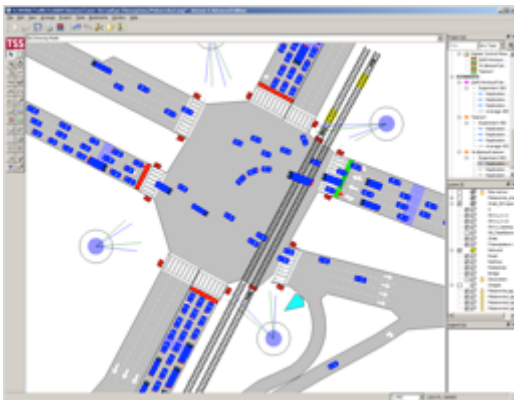
# State-of-the-art: Granularity of traffic models

## Fine-grained

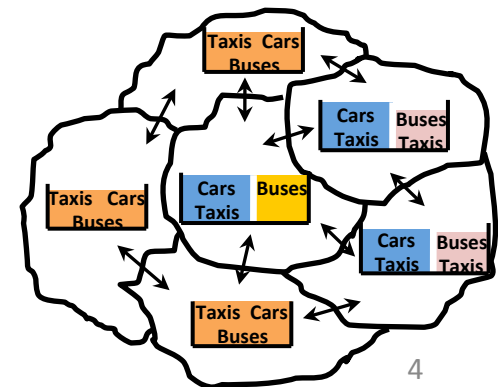
- Data intensive
- Questionable calibration
- Expensive computation
- Unreliable prediction
- Fragmented optimization

## Coarse-grained

- Less accurate
- Lack dynamics
- Non-physical
- Planning oriented



traffic modeling



# State-of-the-art: Traffic optimization & control

Most optimization methods for transport networks

- Fragmented and uncoordinated
- Suited for toy networks with simplified dynamics
- Apply decentralized control
- Micro-simulation and scenario analysis



Cairo



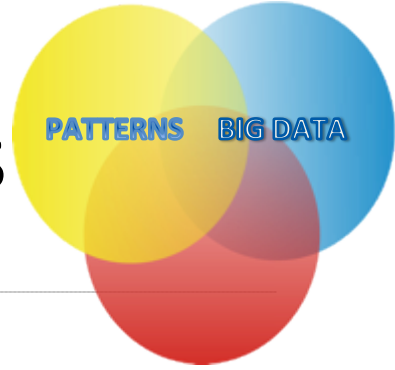
Bangkok



Paris

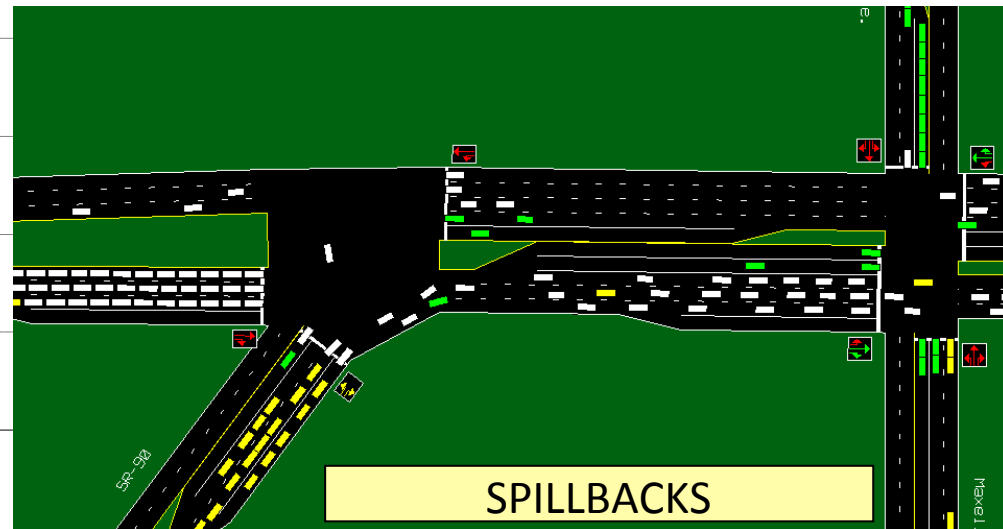
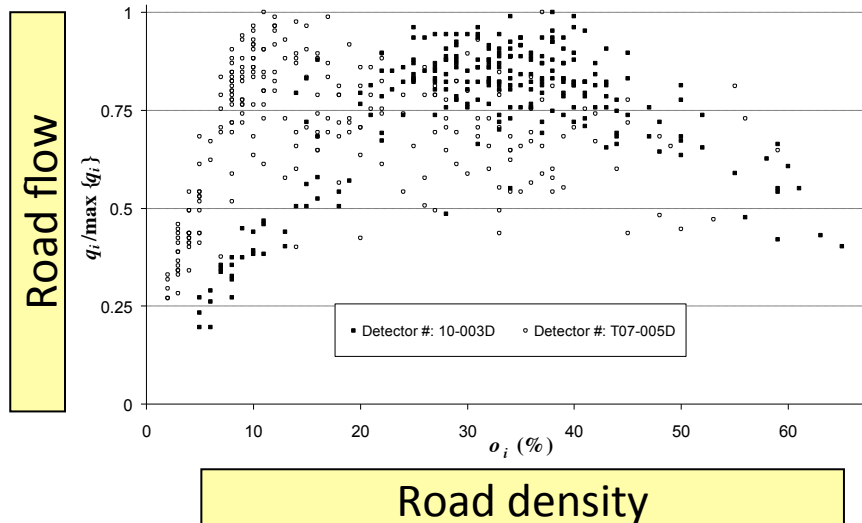
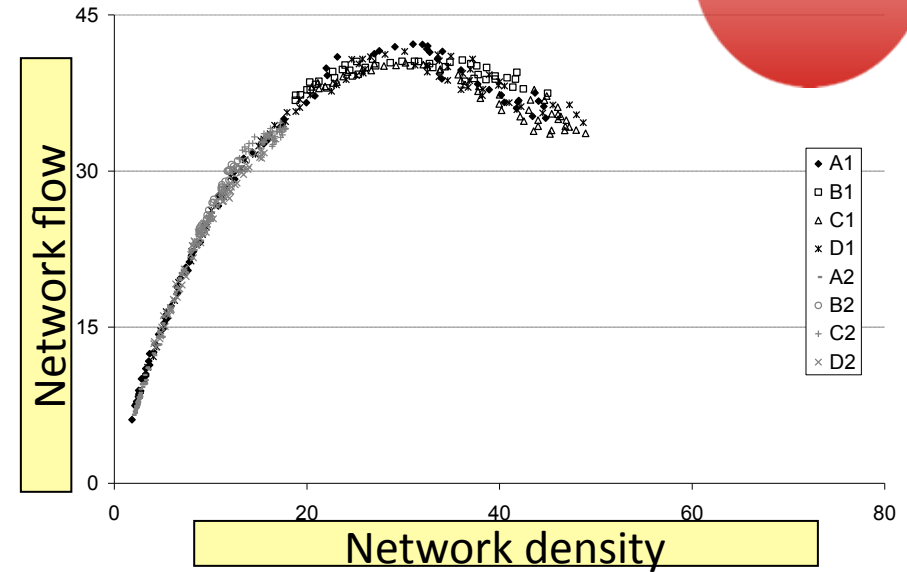
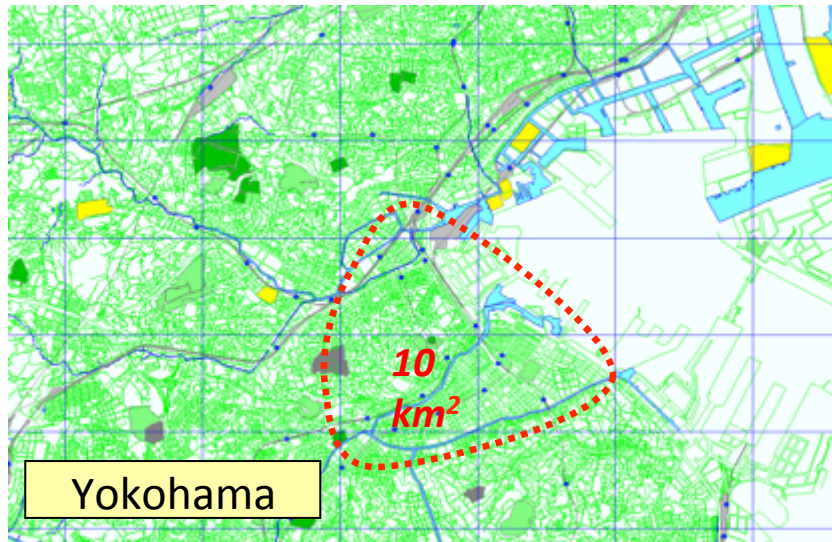


# Network congestion observations



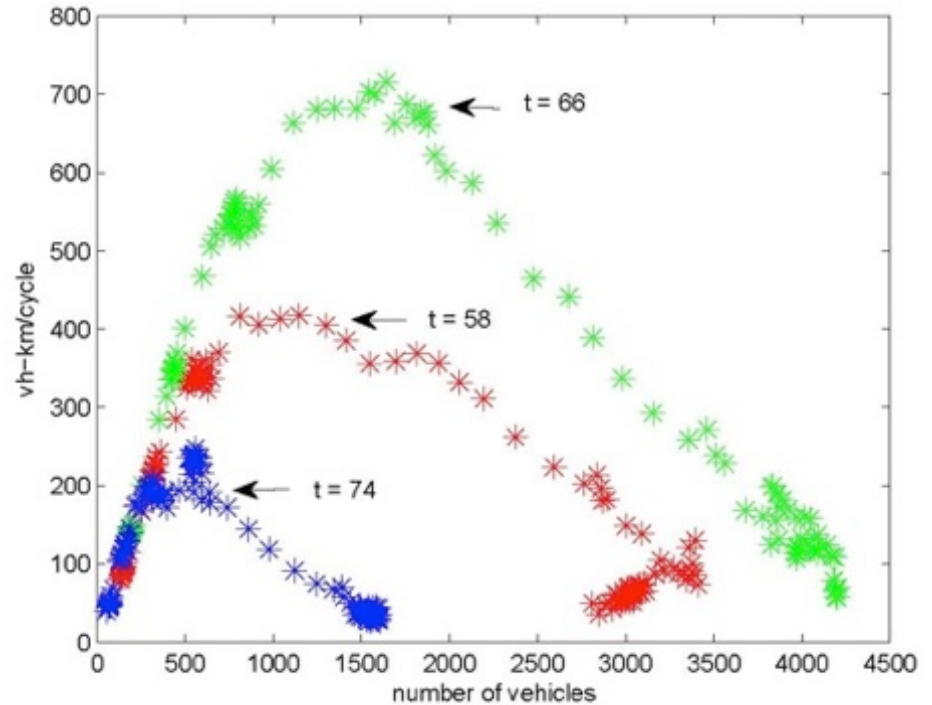
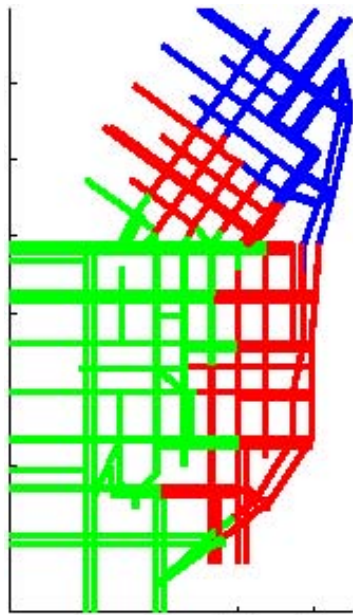
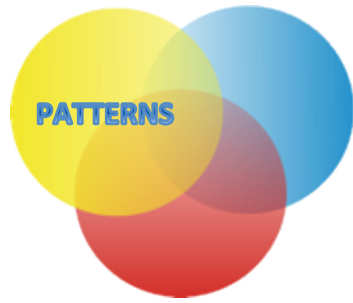
PATTERNS

BIG DATA



Geroliminis and Daganzo (2008) – Trans. Res. Part B

# Clustering – Congestion Dynamics

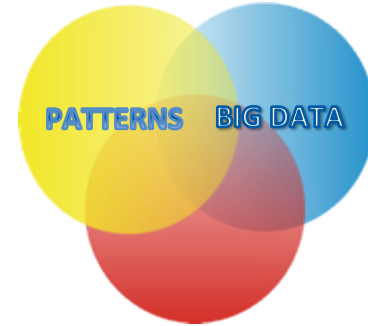
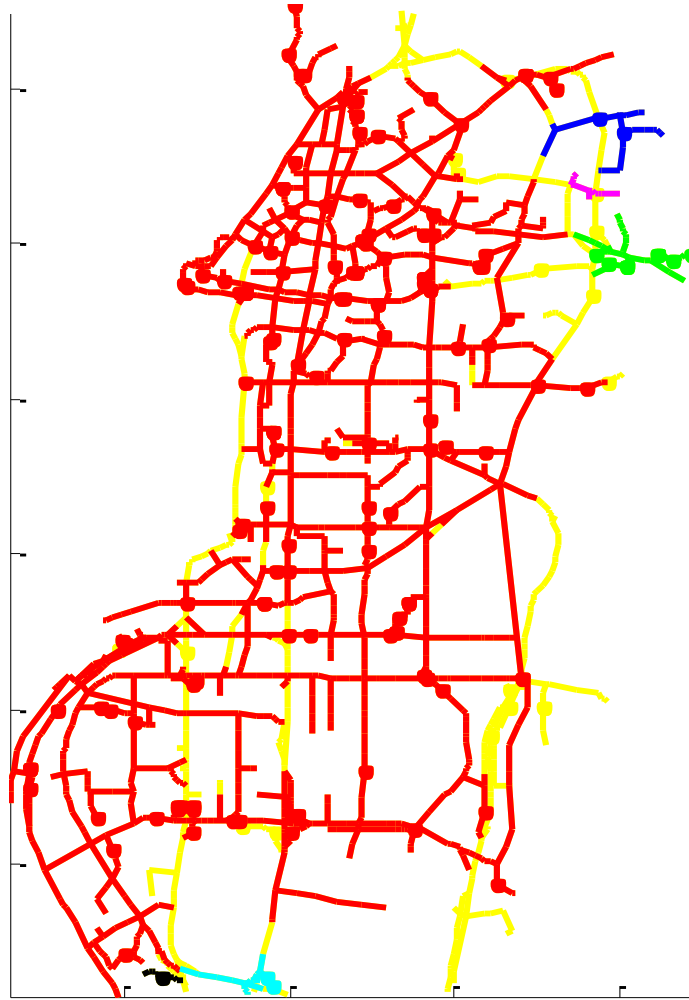


Clusters of a city reach congestion at different times

# Congestion Propagation

Small number of critical pockets of congestion

Significant Spatial correlations



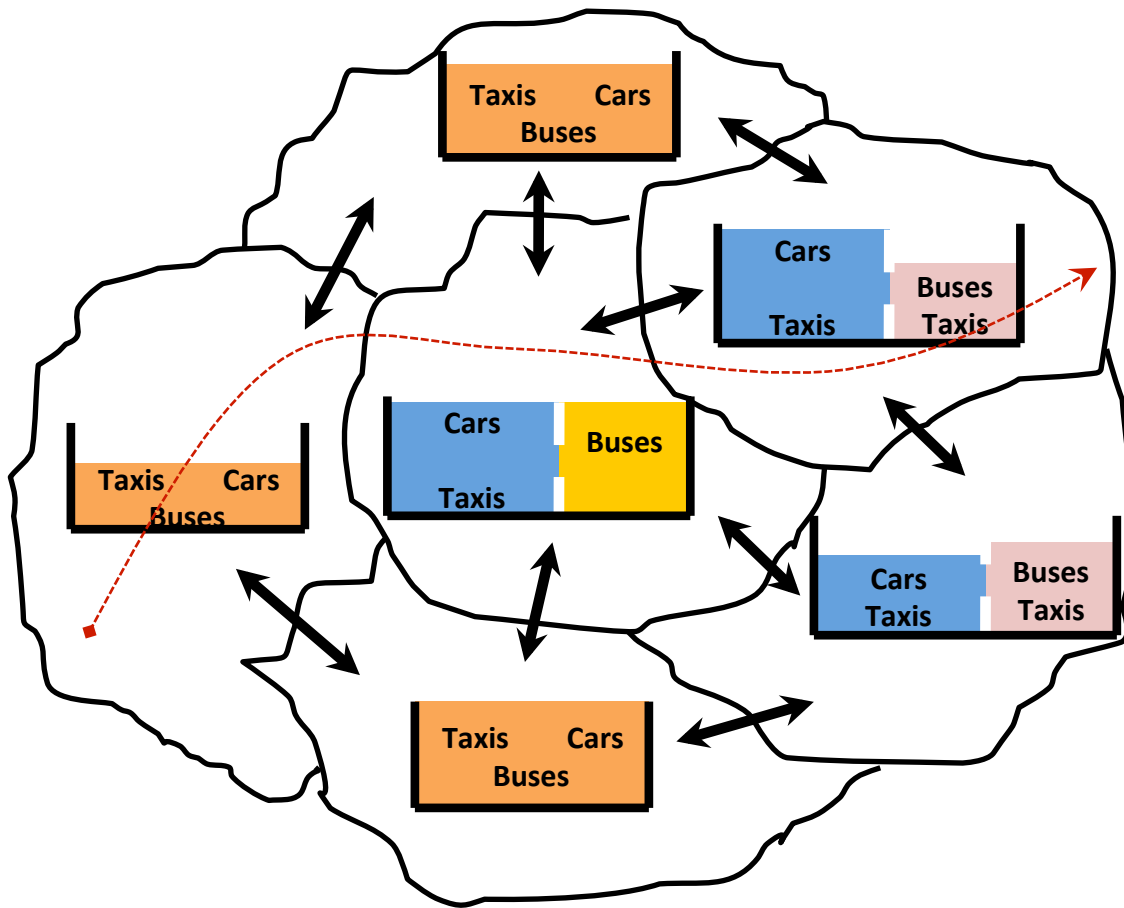
20000 taxis (50M points/day)

9000 links

Shenzhen 12M population



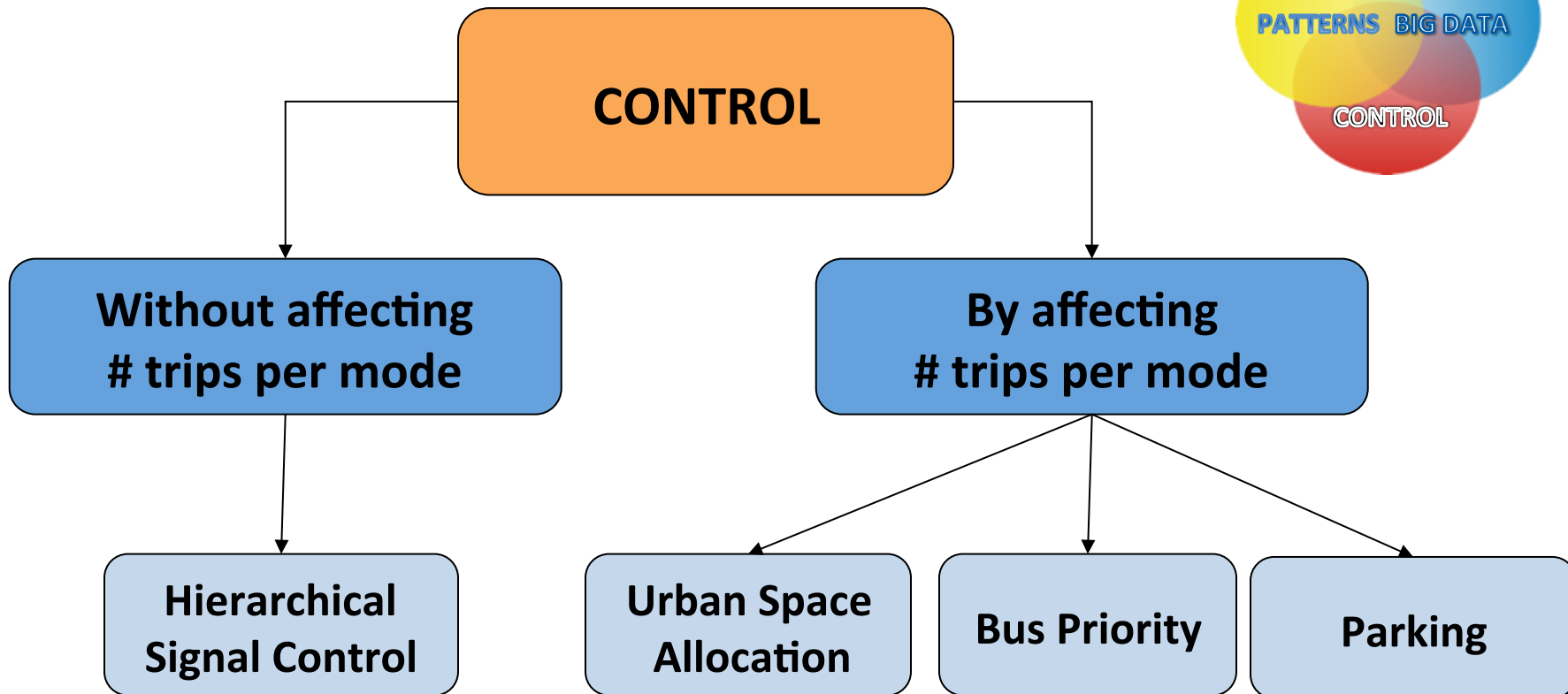
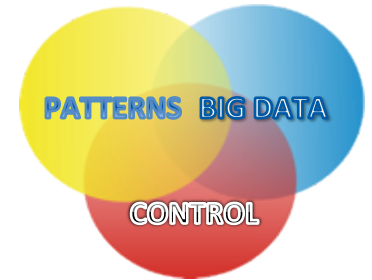
# Multimodal Passenger oriented SoS Vision



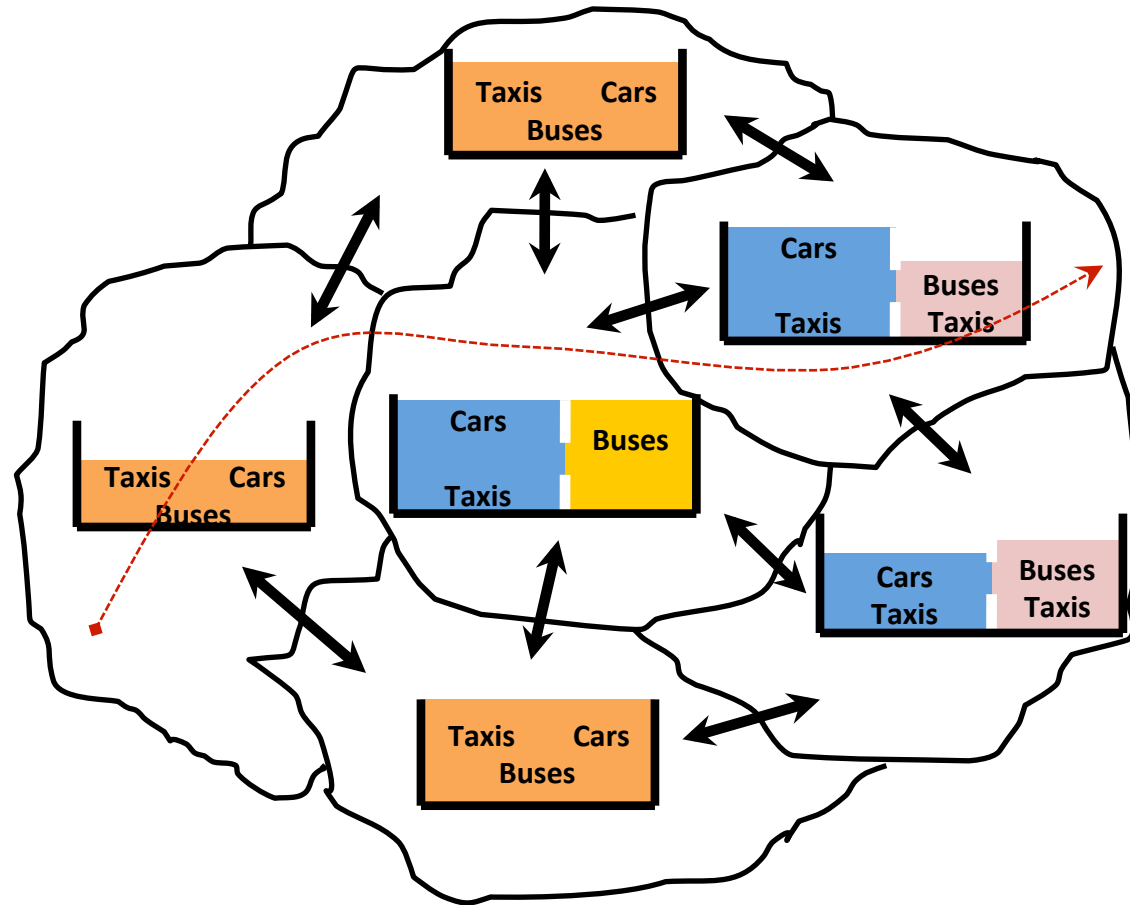
Geroliminis and Boyaci (2012) – Tr. Res. Part B

Zheng and Geroliminis (2013) ISTTT20

# A "System of Systems" Approach

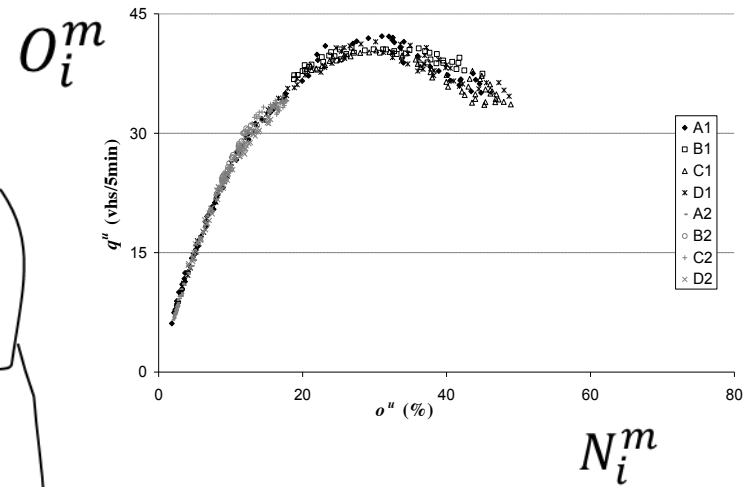
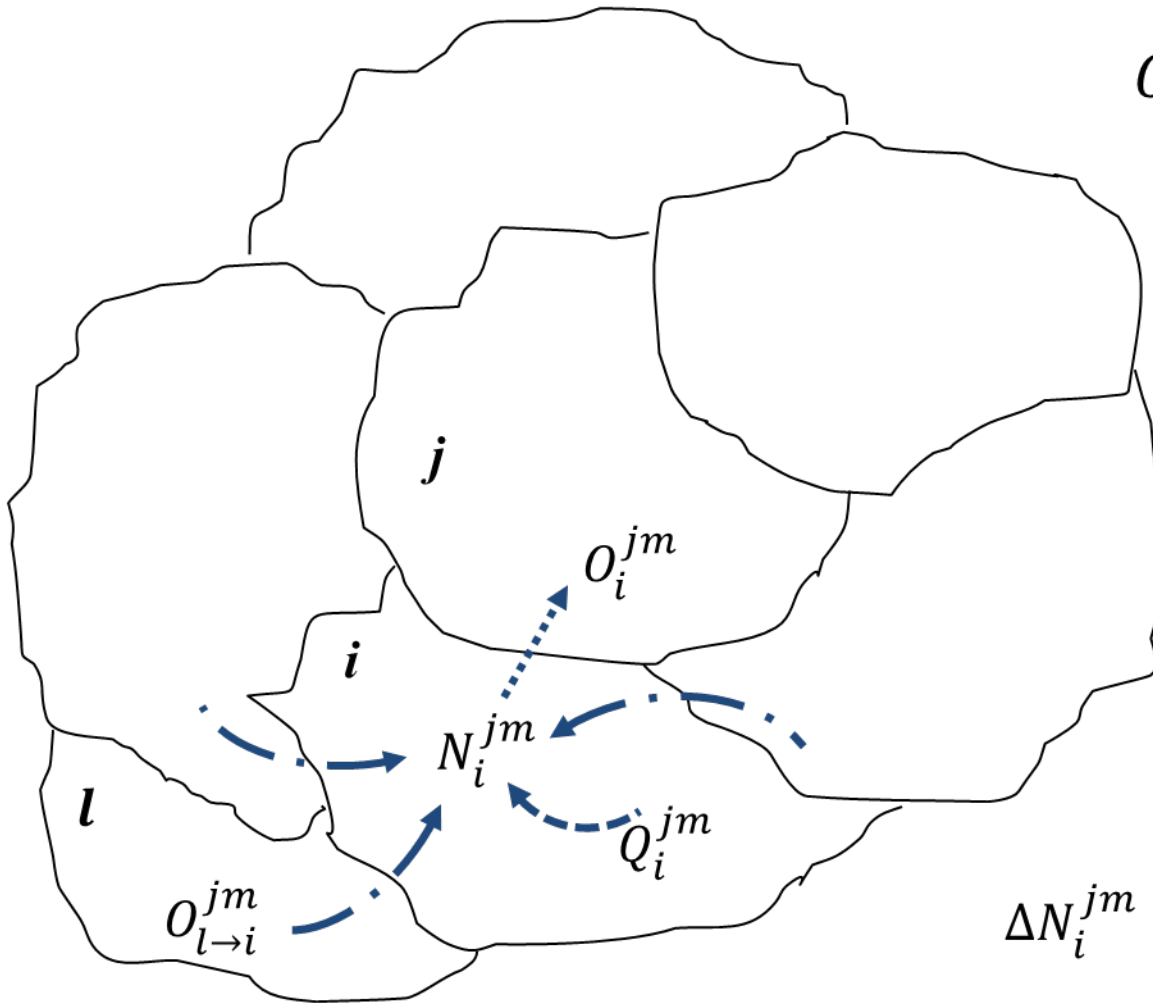


# Multimodal Passenger oriented SoS Vision



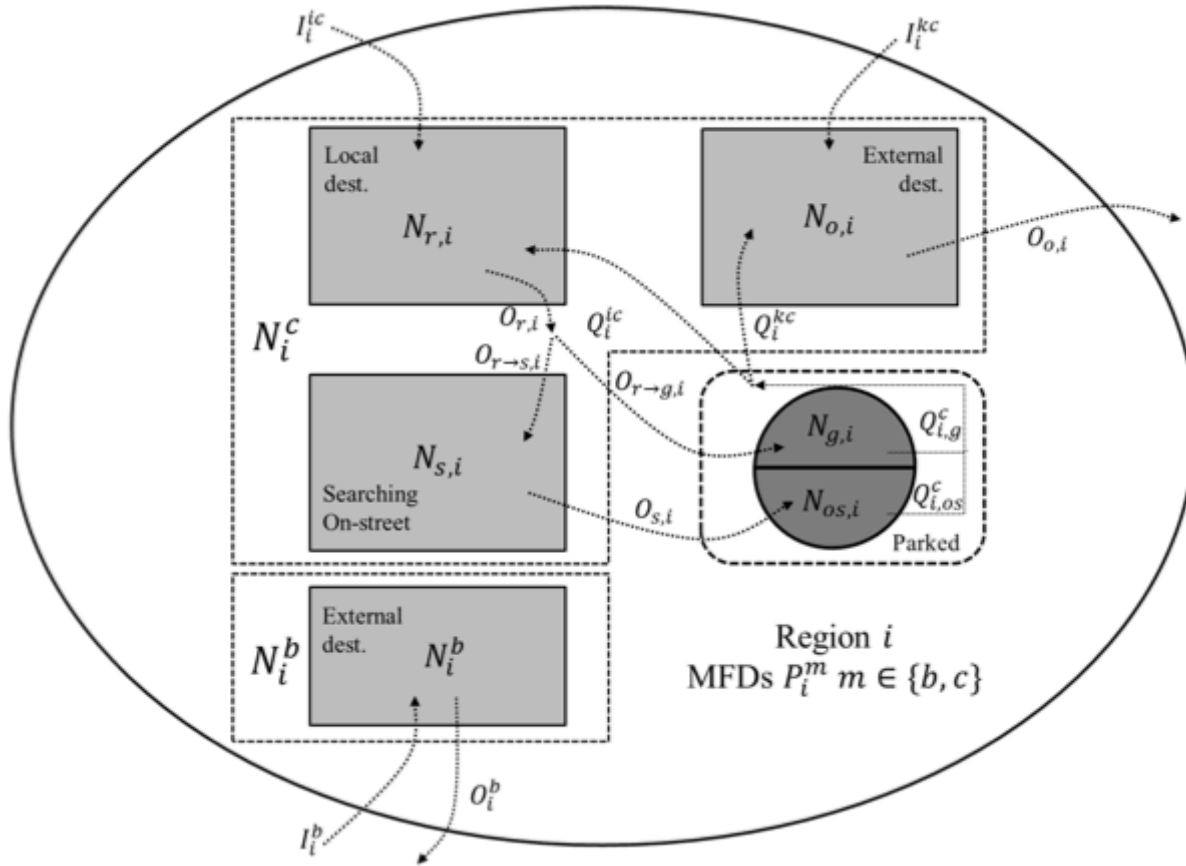


# System dynamics – General representation



$$\Delta N_i^{jm} = Q_i^{jm} + \sum_l O_{l \rightarrow i}^{jm} - O_i^{jm}$$

# Dynamics of one region with cruising



$$N_i^c(t) = \sum_x N_{x,i}(t)$$

$x$ : vehicle activity

$r$ : moving with internal destination

$o$ : moving with external destination

$s$ : cruising

$$O_{x,i}(t) = \frac{N_{x,i}(t)}{N_i^c(t)} \cdot \frac{P_i^c(t)}{l_{x,i}}$$

$$N_{r,i}(t+1) = N_{r,i}(t) + Q_i^{ic}(t) + I_i^{ic}(t) - O_{r,i}(t) \quad (7a)$$

$$N_{s,i}(t+1) = N_{s,i}(t) + O_{r \rightarrow s,i}(t) - O_{s,i}(t) \quad (7b)$$

$$N_{o,i}(t+1) = N_{o,i}(t) + Q_i^{kc}(t) + I_i^{kc}(t) - O_{o,i}(t) \quad (7c)$$

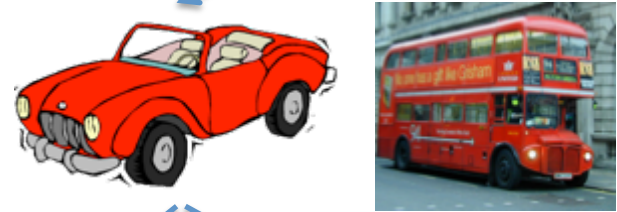
$$N_{os,i}(t+1) = N_{os,i}(t) - Q_{i,os}^c(t) + O_{s,i}(t) \quad (7d)$$

$$N_{g,i}(t+1) = N_{g,i}(t) - Q_{i,g}^c(t) + O_{r \rightarrow g,i}(t) \quad (7e)$$

# Aggregated multimodal choice

- Estimated cost (mode disutility) from real-time

$$c_i^k(t) \begin{cases} \sum_{j \in i \rightarrow k} TT_c^j + p_{os}^k + T_{cru}^k & \text{Car, on-street parking} \\ \sum_{j \in i \rightarrow k} TT_c^j + p_g^k & \text{Car, garage parking} \\ \sum_{j \in i \rightarrow k} TT_b^j + D_b^{i \rightarrow k} + TT_{acc} & \text{Bus} \end{cases}$$



- Nested-logit mode choice

$$\text{Bus share: } \omega_i^b(t) = \frac{\exp(\tau_b \cdot C_i^b(t))}{\exp(\tau_c \cdot C_i^b(t)) + \exp(\tau_c \cdot C_i^c(t))}$$

$$C_i^c(t) = \frac{1}{\beta} \cdot \left( \ln \exp(\beta \cdot C_i^{c,os}(t)) + \exp(\beta \cdot C_i^{c,g}(t)) \right)$$



On-Street  
parking share :

$$\omega_{os,i}^c(t') = \exp(\beta \cdot C_i^{c,os}(t')) / \left( \exp(\beta \cdot C_i^{c,os}(t')) + \exp(\beta \cdot C_i^{c,g}(t')) \right)$$

$$t' = t + TT_c$$

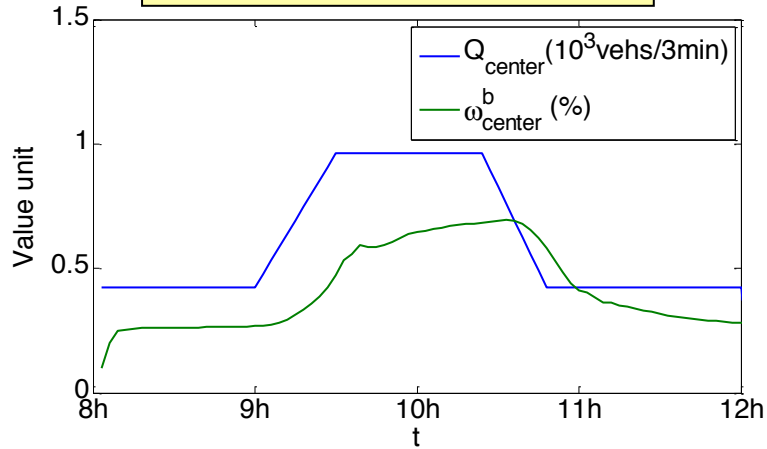


# Pricing Schemes

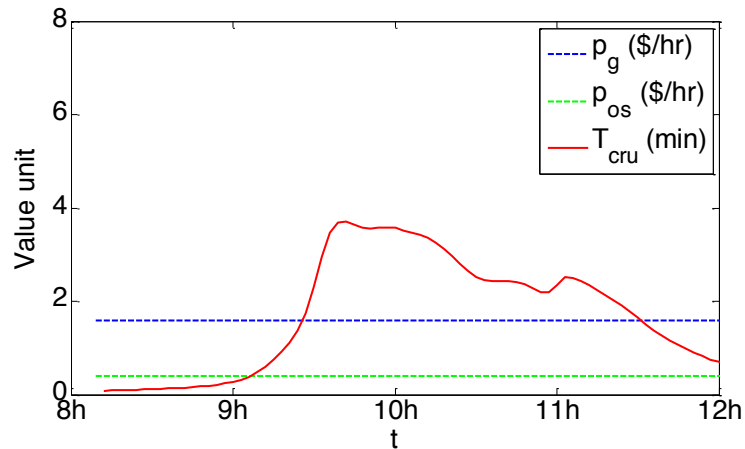
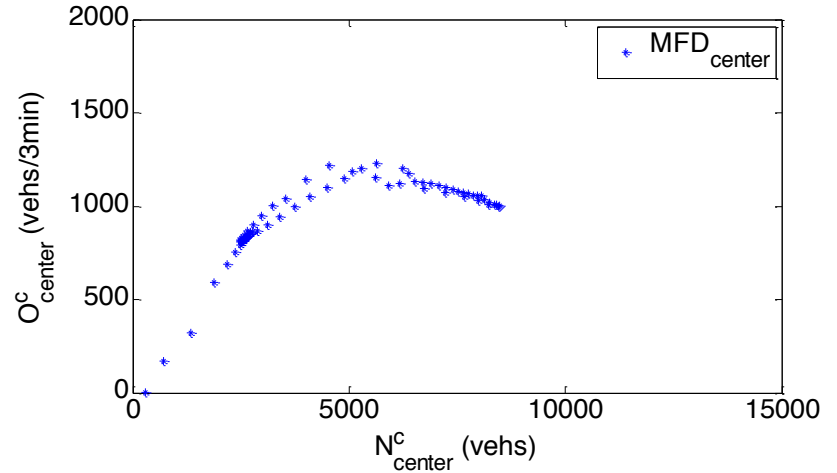
- Pbasic: constant garage pricing, on-street parking is free
- P0: Optimal constant garage and on-street pricing
- P1: System Optimum Pricing
- P2: myopic traffic-responsive pricing
- P3: Pricing competition between on-street and garage

# System performance: flat-rate pricing (P0)

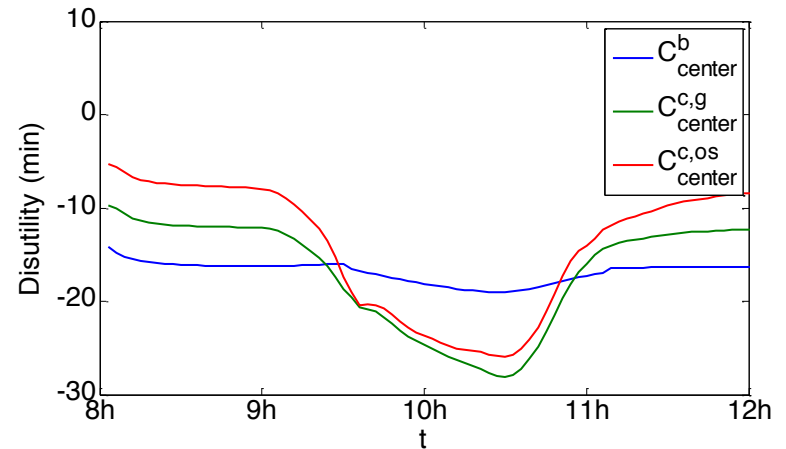
Demand & Mode split



MFD center region



Fixed Pricing &  
Resultant cruising time



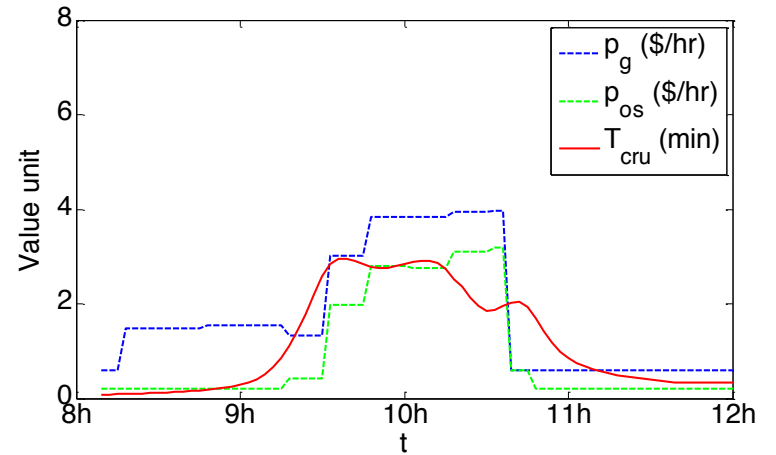
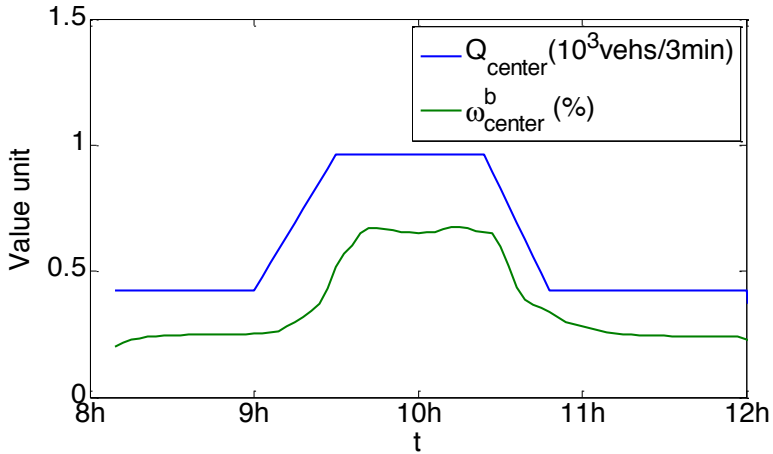
Cost per mode

# System Optimum Pricing (P1):

$n_i$   $n_i$   $\Delta m, t, l$   $\Psi$

Earlier mode shift  
Higher bus share

Time-dependent Pricing &  
25% less cruising time





# Congestion-responsive pricing (P2)

## □ Control objective:

- Maintain general congestion level below  $N^{cr}$
- Maintain cruising congestion level below  $N^{sT}$

## □ PI-type feedback control strategy

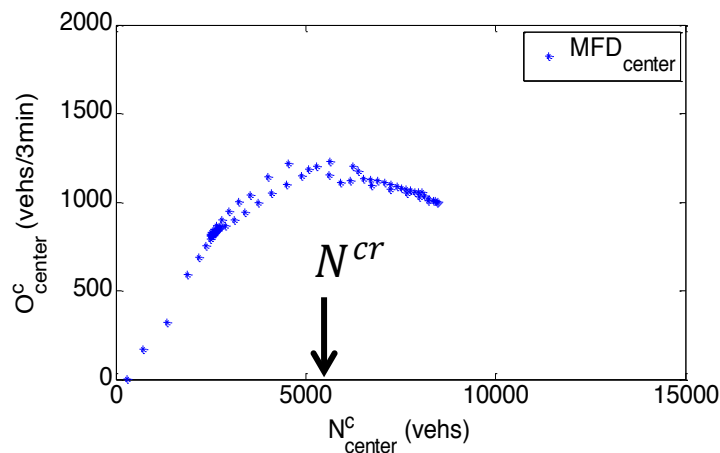
$$p_g(t+1) = p_g(t) + c_1(N^c(t) - N^{cr})$$

- Price, garage

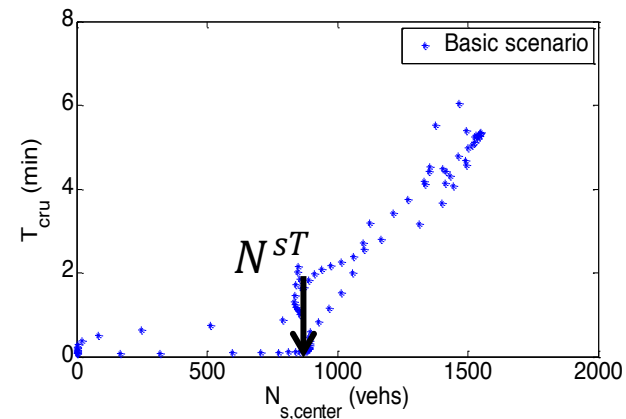
$$p_{os}(t+1) = p_{os}(t) + c_1(N^c(t) - N^{cr}) + c_2(N_s(t) - N^{sT})$$

- Price, on-street

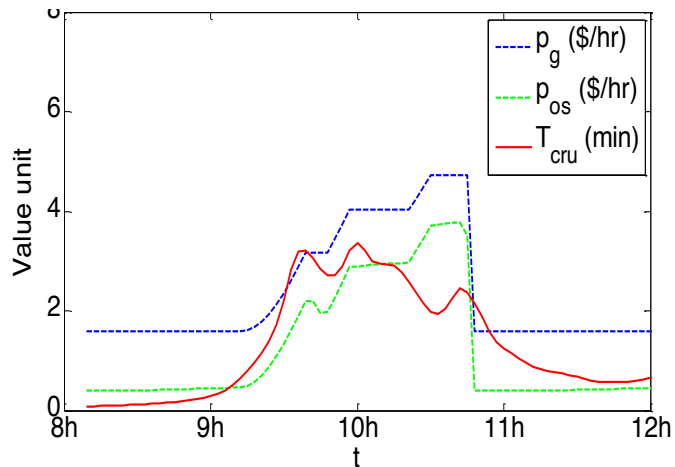
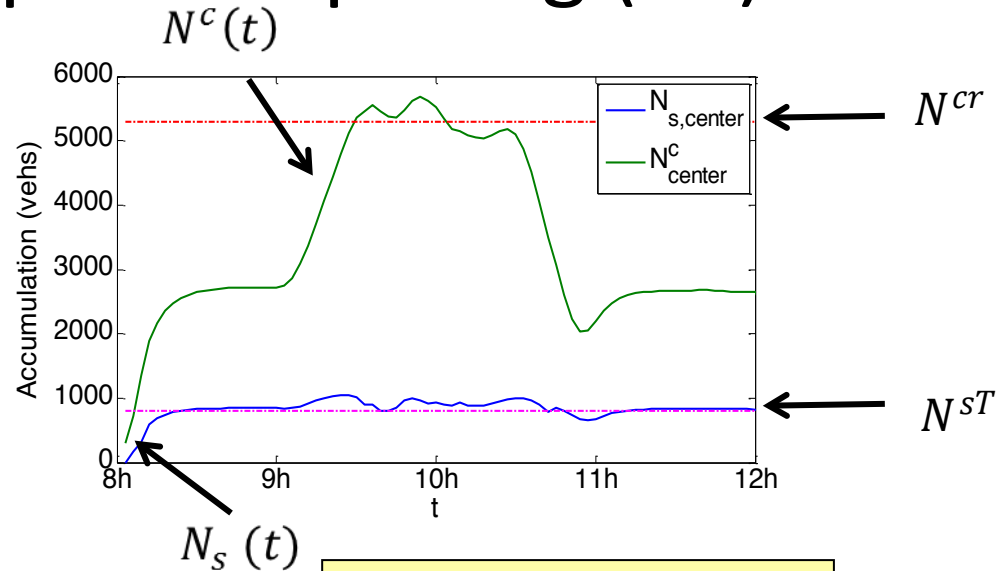
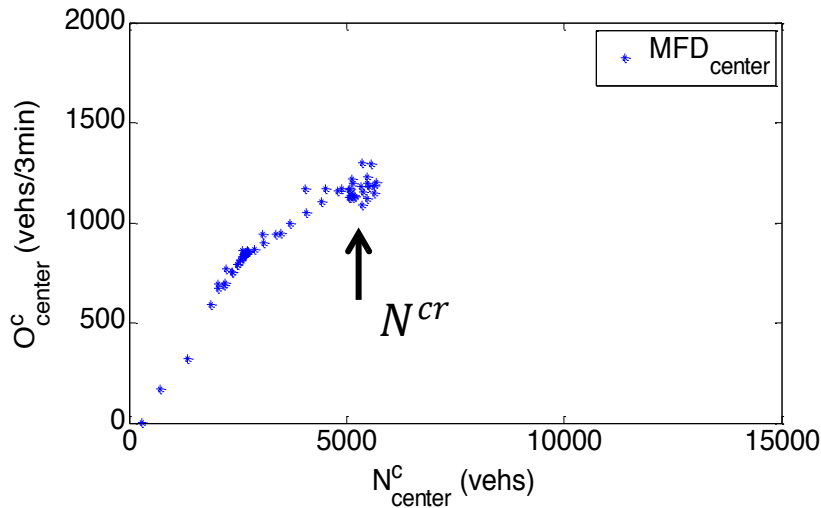
MFD (center region)



Cruising time vs. searching vehicles



# Congestion-responsive pricing (P2)



	Saving in PHT (hrs)	Total toll (hrs)	Toll efficiency (PHT.sav/Total Toll)	Ave. cruising delay (min)
Base scenario	0	660	0	3.7
Strategy P1	1211 (2.7%)	2641	45.8%	1.9
Strategy P2	5944 (13.0%)	7207	82.5%	1.4
Strategy P3	6990 (15.5%)	5857	119.5%	1.2

Pricing and cruising over time

# Parking price competition (P3)

## □ Operators and objectives

$$\text{City manager} \quad : \quad \min_{p_{os}(t)} TPC = \sum_{t,i,m} (PHT_i^m(t) + Tos_i^c(t) + Tg_i^c(t))$$

$$\text{Garage company:} \quad \max_{p_{og}(t)} BG = \sum_{t,i} Tg_i^c(t)$$

*PHT: total travel time*

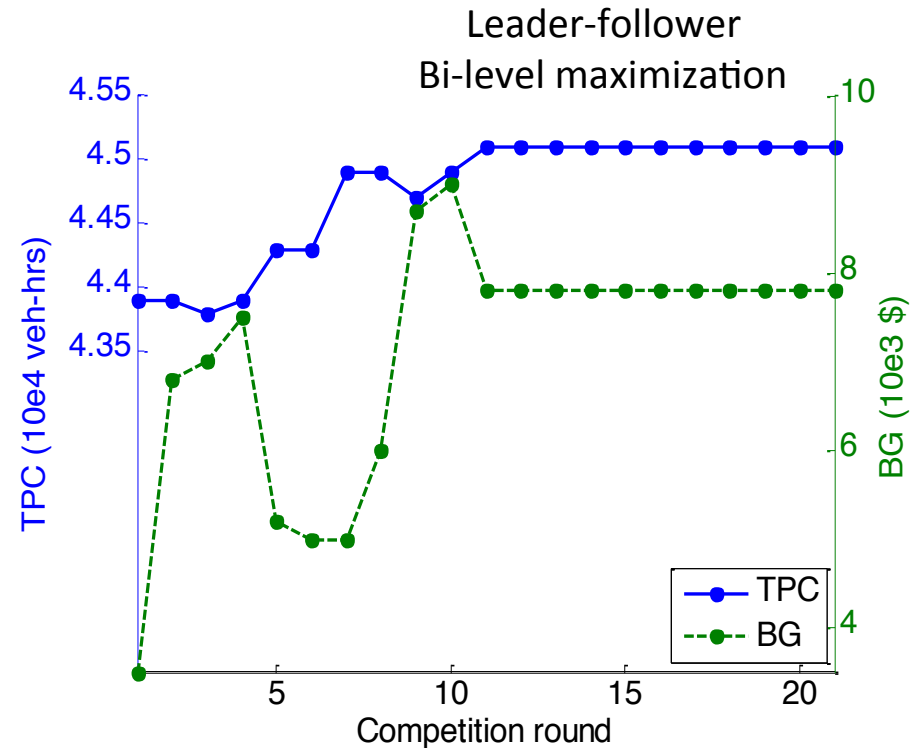
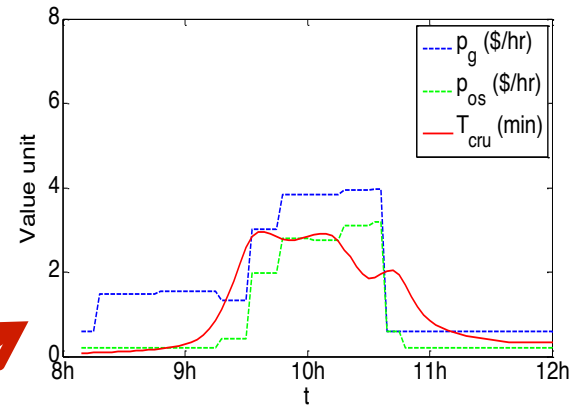
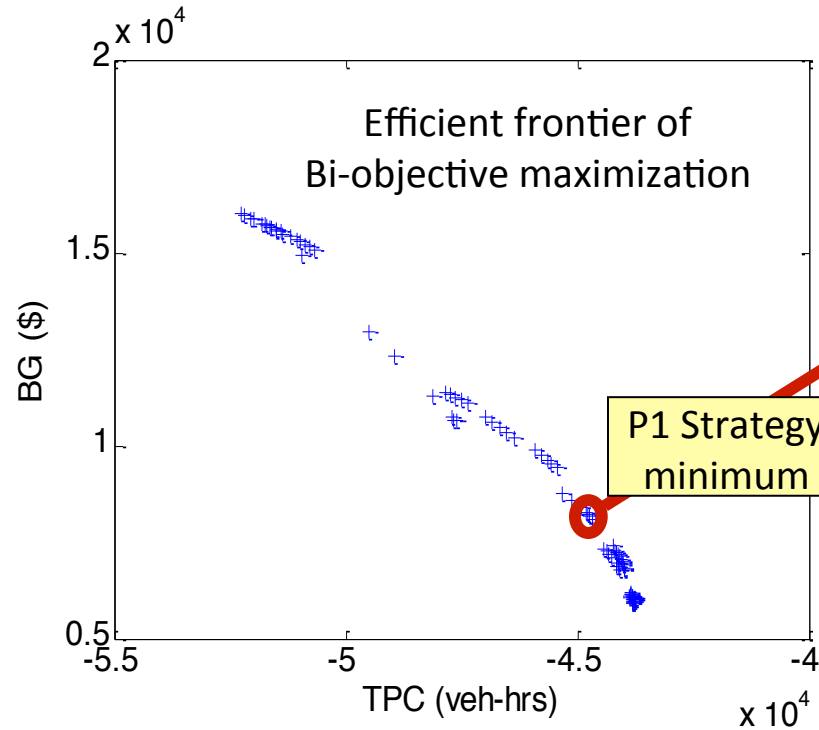
*Tos: total toll paid, on-street parking*

*Tg: total toll paid, garage parking*

## □ Competition scenarios

- Cooperation: maximize the common benefit
- Individual maximization: change prices knowing the other's

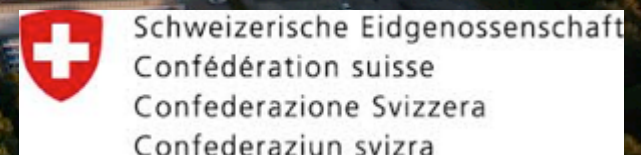
# Parking price competition – Preliminary results



# RESEARCH SPONSORS



Transport  
Roads & Maritime  
Services





# DISCUSSION

- Parking research deserves attention, as everybody needs a spot

